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pH dependent *C. jejuni* thermal inactivation models and application to poultry scalding

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1. Introduction

Campylobacter jejuni, a major cause of foodborne illness, continues to cause millions of cases of illness in humans (e.g. gastroenteritis) annually. An estimated 20–150 cases are reported per 100,000 people in industrialized nations each year (Olson et al., 2008). A primary driver is consumption of undercooked poultry products (FAO/WHO, 2009). Modern studies report *Campylobacter* prevalence of retail poultry carcasses to be 57.7% in Canada, 58.8% in Japan, and 90% in the United Kingdom (Suzuki and Yamamoto, 2009; Moran et al., 2009). Furthermore, an estimated 24% and 46% of processors will be unable to pass stricter 2015 FSIS-USDA *Campylobacter* performance standards for raw chicken carcasses and not-ready-to-eat communicated chicken parts, respectively (US Department of Agriculture and Service, 2015).

While *C. jejuni* originates in the gastrointestinal tract of poultry,

each bacterium finds its way onto the skin and feathers through external means (FAO/WHO, 2009). Birds are contaminated externally due to excreta buildup in densely populated living conditions. Contamination may not be eliminated during processing before retail sale and consumption. Of steps bringing a live chicken to retail, the slaughterhouse is a site of concern. The scalding process has been identified as a site providing opportunity for cross-contamination by the World Health Organization (FAO/WHO, 2009). In addition, cross-contamination between birds has been shown to be highly prevalent in scalding (Mulder et al., 1978).

Scalding background: Scalding is one of many stages in the poultry process. Typically, it is conducted immediately after chickens have been killed and bled out. As the first cleaning stage of poultry processing, bacteria and organic material levels are among the highest prior to scalding (FAO/WHO, 2009). Hence the opportunities for cross-contamination are abundant in this early processing stage. The two methods of scalding currently used in large-scale processing plants are *immersion* and *steam*, where the former is most widely adopted and the main focus of this work. During a

typical two minute immersion scald, birds are immersed in 50–60°C aerated (scald) water to prepare birds for defeathering, wash off dirt and organic material, and reduce bacteria levels. Many foodborne pathogens associated with poultry, including *C. jejuni*, are heat sensitive and are inactivated thermally in the scalding temperature range (FAO/WHO, 2009).

Chemical additives in scalding: It is popular among poultry processors to utilize chemical additives and antimicrobials in scald water to enhance the killing of bacteria. By altering water chemistry and pH, the rate of bacterial inactivation also changes. However, conflicting experimental results on the efficacy of chemical additives indicate a more detailed understanding of the bacterial inactivation process may prove useful in pathogen control. We invite the reader to see our review of experiments using additives including bacteria counts and prevalence in AppendixA (Lillard et al., 1987; Okrend et al.; Humphrey and Lanning, 1987; Berrang et al., 2011).

In order to gain predictive insight on how scald water temperature and pH affect the inactivation of *C. jejuni*, we construct and utilize mathematical models. The power here is that, along with industrial scale data, such models can test mechanistic hypotheses as well as provide quantifiable connections between processing parameters and resulting bacteria levels in both the scald water and on chicken carcasses. In light of this perspective, the paper is organized as follows: first, in Section 2, we develop an inactivation model linking pH and temperature to death rates of *C. jejuni* in scald water using recent experimental data. Second, in Section 3, we present a mathematical model describing inactivation and transfer of *C. jejuni* in the immersion scalding process. In Section 4, we validate our findings by successfully predicting experimental bacteria counts in scald water using the model developed herein. Also, we provide general guidelines for combating cross-contamination and improving overall microbiological quality at the scalding stage. In Section 5 we discuss the affects of pH and temperature on cross-contamination using the steady-state concentration of bacteria in scald water (see Section 5.1). Furthermore, we illustrate the applicability and relevance of our work by using Canadian processor survey data to give alternative scalding strategies and operating conditions (see Section 5.3). Finally, we provide directions for further study and call for specific future experiments needed to fill gaps in present knowledge and data (see Section 5.4).

2. Thermal inactivation of *C. jejuni*

2.1. Experimental results

The time to kill 90% of an initial population is called a decimal reduction time, or *D-value*. All available experimentally determined

C. jejuni D-values across six experiments have been compiled for this study, totaling 17 *C. jejuni* strains (Al Sakkaf and Jones, 2012; Doyle and Roman, 1982; Sörqvist, 1989; Blankenship and Craven, 1982; Waterman, 1982; Nguyen et al., 2006). These D-values give the killing rate of *C. jejuni* in neutral pH media such as brain-heart infusion broth (BHI) and skim milk. The high variation in killing rate with temperature is captured in Fig. 1A. While suspension temperature is crucial, pH also plays a pivotal role in bacteria inactivation (Bazin and Prosser, 1988; Humphrey and Lanning, 1987). As pH drifts away from neutral to acidic or alkaline, the rate of killing is increased (Bazin and Prosser, 1988). In other words, neutral pH 7 is the highest point of thermal resistance (Bazin and Prosser, 1988). Experimental results of *C. jejuni* D-values across the pH spectrum are shown in Fig. 1B. To further complicate the situation, scald water contains high levels of organic material (e.g. excreta, blood, fat, proteins, etc.), buffering the bacterial inactivation process (Humphrey and Lanning, 1987; Yang et al., 2001). If the processor accounts for the least sensitive strain (highest thermal resistance), then the remaining strains will also be inactivated. In Section 2.2, we provide an effective range which covers a wide variety of strains regardless of their individual thermal resistances. We invite the reader to see a more complete discussion regarding these items in AppendixB.1 and AppendixB.2.

2.2. Determining inactivation rate during scalding process

To gain insights into the scalding process, we develop a model accounting for the items mentioned above. Specifically, we wish to address:

- 1) The variation across experiments in killing rate versus temperature (Fig. 1A)
- 2) The effects of pH on thermal inactivation (Fig. 1B)
- 3) The buffering effects of organic material present in scald water (Yang et al., 2001).

To capture the combined effects of pH and temperature on D-values in scalding water, relative to each of the 17 *C. jejuni* strains from the available data, we propose the following inactivation model:

$$D_{w_i}(pH, T) = D(pH)[D_i(T)] \quad (1)$$

where *i* refers to a particular *C. jejuni* strain, *T* is the temperature of the scald water, and the forms of *D(pH)* and *D_i(T)* are dictated by experimental data (see Fig. 1A and B). In particular, we use *D(pH)* =

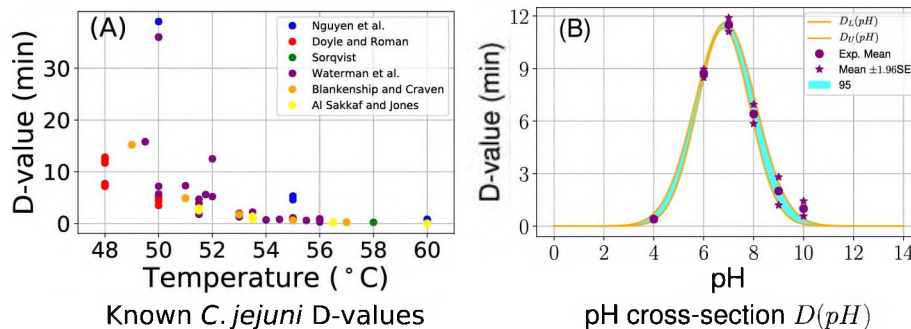


Fig. 1. (A) All known *C. jejuni* D-values with respect to temperature (Al Sakkaf and Jones, 2012; Doyle and Roman, 1982; Sörqvist, 1989; Blankenship and Craven, 1982; Waterman, 1982; Nguyen et al., 2006). D-values from a given paper are assigned the same color. High D-value variation is seen especially at low temperatures. As temperature increases, D-value variation appears to decline. (B) Experimental *C. jejuni* D-values taken in 52°C scald water with 13 mg/ml total solids and 6.2 mg/ml proteins (Humphrey and Lanning, 1987). The filled region represents a 95% confidence interval for the *C. jejuni* D-values as suspension pH varies. For data fitting details see AppendixB. (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

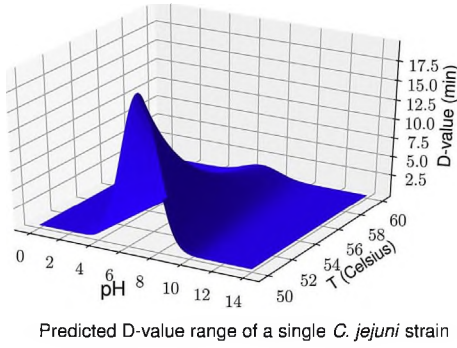


Fig. 2. Displayed is the predicted D-value range for a single *C. jejuni* strain, a building block of our inactivation model $D_w(pH, T)$. Essentially the cross-sections from a single strain's D-values vs. temperature with the D-value vs. pH cross-sectional area are combined in Fig. 1B. This can be seen by the Gaussian shape with pH and decaying exponential in temperature. By repeating this process for each of the 17 *C. jejuni* strains in Fig. 1A, we see lower and upper bounding surfaces arise naturally. Allowing $D_w(pH, T)$ to take all values between these lower and upper bounds takes into account all known experimental variation in *C. jejuni* kill rates, suspension pH effect on kill rate, and buffering effects of organic material present in scald water.

$\hat{a}e^{-((pH-b)/c)}$ and $D_i(T) = a_i e^{b_i(T-T_{ref})}$. In order to determine the parameters \hat{a} , \hat{b} , \hat{c} , a_i , and b_i , we use the data illustrated in Fig. 1A and B to solve the respective least squares problems for $D_i(T)$ and $D(pH)$ (Humphrey and Lanning, 1987; Al Sakkaf and Jones, 2012; Doyle and Roman, 1982; Sorqvist, 1989; Blankenship and Craven, 1982; Waterman, 1982; Nguyen et al., 2006). Notice that for D-values as a function of pH, we use the upper and lower bounds of the 95% CI to solve the inverse problem for $D_U(pH) = a_U e^{-((pH-b_U/c_U))^2}$ and for $D_L(pH) = a_L e^{-((pH-b_L/c_L))^2}$ (illustrated by the upper and lower curves, respectively in Fig. 1B).

In order for model (1) to be relevant during scalding, we scale the fitted parameters a_i to be 1 so that

$$D_L(pH) \leq D_{wi}(pH, T_{ref}) \leq D_U(pH). \quad (2)$$

With this scaling of a_i and setting $T_{ref} = 52^\circ\text{C}$, we impose the condition that model (1) determined D-values agree with the cross-section illustrated in Fig. 1B. The motivation for this is as follows: since the D-value vs. pH experiments take place in actual scald water at 52°C with high concentrations of organic material and proteins, we scale the $D_i(T)$ equation to agree with this data. These ideas are displayed graphically in Fig. 2. We repeat this process for all 17 *C. jejuni* strains; and, arising naturally are lower and upper bounds due to the spread in experimental data. To capture this experimental variation, we consider all D-values between the upper and lower bounds. For each pH and temperature pair, $D_{wi}(pH, T)$ gives precisely this full range of *C. jejuni* D-values and addresses key items 1), 2), and 3) above. For the rest of the paper, instead of referring to D_{wi} in (1) for all 17 strains, we use the notation D_w to account for the relevant range of inactivation values across all 17 strains. For more mathematical, data fitting, and model construction details concerning (1), please see AppendixB.3.

2.3. Validation of inactivation model at $T_{ref} = 52^\circ\text{C}$

Using data from two experimental results which estimate *C. jejuni* D-values taken from an industrial scald tank after four hours of continuous processing (Okrend et al.), we provide forward validation for model (1) at $T_{ref} = 52^\circ\text{C}$ for two different pH values. In scald water at pH 6.97 a D-value of 10.93 ± 2.87 min was reported at 52°C (Okrend et al.). At this temperature and pH value, model (1) predicts a D-value range of $D_w(6.97, 52) = [11.14, 11.57]$ min. Furthermore,

in scald water treated with acetic acid (pH 4.38), a D-value of 1.20 ± 0.45 min was estimated at 52°C (Okrend et al.). Our inactivation model (1) predicts a D-value range of $D_w(4.38, 52) = [0.81, 1.45]$ min. Thus, in the case of $T_{ref} = 52^\circ\text{C}$, model (1) predictions show good agreement with the D-values determined from (Okrend et al.). Note that the data from (Okrend et al.) is not part of the original data sets from which model (1) was developed. What remains to be shown is the predictive capacity of model (1) at temperatures other than $T_{ref} = 52^\circ\text{C}$ in the context of industrial scalding. To do so, we develop a model for the scalding process that incorporates the inactivation model (1) as a key component.

3. Scald model

In this section we develop a scald model, based on a system of ordinary differential equations, in the context of an industrial setting that quantifies (i) bacteria levels in the scald water and (ii) bacteria levels on the surface of the carcasses. Models of this form have been successfully used to predict bacteria counts in process water at other stages of the poultry processing chain (e.g. immersion chilling (Munther et al., 2016; McCarthy et al., 2017; Sukted et al., 2017)). The incoming rate of carcass mass in kg/min is N and carcasses leave the scald tank at rate d_s (1/min), i.e., $1/d_s$ is the scald tank mean residence time in minutes. The mass of carcasses in the scald tank is assumed to be constant at $P = N/d_s$ (kg) after $1/d_s$ min of scalding operation. Note that scald time, or duration, is typically 1–2 min. Lastly, the scald tank has volume T_V (liters).

The viable *C. jejuni* averaged over all resident scald carcasses is given by v_p (CFU/carcass). Bacterial loads vary from carcass to carcass, so we consider an average load over all incoming carcasses σ (CFU/kg) to be constant. While there is variation of input contamination due to transmission within flocks and also between flocks (FAO/WHO, 2009), we assume an average over all these variations σ is constant. With the average contamination σ and a constant rate of carcasses entering the tank, the rate of incoming viable bacteria may be written σN , where m_c is the mass of a typical broiler chicken. We also consider bacteria shedding from carcass surfaces to scald water at rate k_{cw} (1/min) and thermal inactivation on carcass surfaces at rate I_c (1/min). Hence we have $\dot{v}_p = \frac{m_c \sigma N}{P} - k_{cw} v_p - I_c v_p - d_s v_p$, where $\dot{\cdot}$ indicates the derivative with respect to time.

Our model also considers viable bacteria in scald water W (CFU/ml). Bacteria shedding from surfaces of carcasses to the water occurs at rate $\frac{k_{cw} v_p P}{10^3 T_V m_c}$. Bacteria present in scald water is inactivated at rate I_w (1/min). Because I_w depends on both the pH and temperature of the scald water in question, we utilize model (1), defining $I_w = \ln(10)/D_w(pH, T)$. Thus, I_w reflects a range, determined by $D_w(pH, T)$, which contains the effective kill rate of *C. jejuni* in scald water at a fixed pH and temperature. Finally, scald water overflow (and replenishment) occurs at rate g (L/min), indicating that bacteria leave at rate g/T_V (1/min). Putting these pieces together, we have $\dot{W} = \frac{k_{cw} v_p P}{10^3 T_V m_c} - I_w W - \frac{g}{T_V} W$. The bacteria in the scald tank is taken to be initially zero as no carcasses have entered at $t = 0$. Similarly, we assume that no bacteria are present in the scald water prior to scalding. As a result we impose the initial conditions $v_p(0) = 0$ and $W(0) = 0$ for the following system:

$$\begin{cases} \dot{v}_p = \frac{m_c \sigma N}{P} - k_{cw} v_p - I_c v_p - d_s v_p, & v_p(0) = 0, \\ \dot{W} = \frac{k_{cw} v_p P}{10^3 T_V m_c} - I_w W - \frac{g}{T_V} W, & W(0) = 0, \\ I_w = \ln(10)/D_w(pH, T). \end{cases} \quad (3)$$

3.1. Model properties and steady states

The scald model (3) is well-posed mathematically. In other words, we have existence and uniqueness of solutions for (3). It can easily be shown that for non-negative initial conditions, solutions may be found which remain positive and bounded. Therefore solutions associated with non-negative initial conditions capture relevant bacterial levels in time. Note that model (3) is linear, hence closed form solutions may be easily found. In particular, we are interested in the steady states of model (3). The unique positive steady state of (3), (v_p^*, W^*) is given below in (4). Using standard techniques, this steady state can be shown to be globally asymptotically stable for biologically relevant solutions (i.e., solutions associated with non-negative initial conditions).

$$\begin{aligned} v_p^* &= \frac{m_c \sigma N}{P(k_{cw} + I_c + d_s)} \\ W^* &= \frac{k_{cw} v_p^* P}{10^3 T_V m_c \left(I_w + \frac{g}{T_V} \right)} \end{aligned} \quad (4)$$

Since the data used to validate scald model (3) (see Section 4) is taken from an industrial scald operation that is at steady state, (4) is instrumental in the analysis that follows (Osiriphun et al., 2012).

3.2. Scald process parameters

Model (3) is constructed from two main types of mechanisms: (I) those that involve typical processing procedures for industrial scalding and (II) bacteria transfer and inactivation. Parameters, along with relevant values/ranges, corresponding to Type I or Type II mechanisms are categorized below. Parameter values/ranges are determined from a relatively complete set of scalding tank specifications and experimental *C. jejuni* counts from a plant in Thailand (Osiriphun et al., 2012).

Determination of Type I parameters: Scalding specifications are as follows: scald water pH is 8, tank volume T_V is 5900 L, scald water overflow rate g is 172 L/min, and carcass residence time in the scalding tank is 1.85 min (Osiriphun et al., 2012). Since carcass residence time is 1.85 min, the rate at which carcasses leave the scalding tank is $1/1.85$ min, i.e. $d_s = 1/1.85$ (1/min). We find incoming carcass mass N using line processing speed and average carcass mass m_c . Line speed is reported to be 200 birds per minute (Osiriphun et al., 2012). Although carcass mass is not reported, typical broiler carcass mass is 2 kg. As a result $N = 200m_c = 400$ kg/min. Note that experiments were conducted with scald water at 54.15°C (Osiriphun et al., 2012). For the remainder of Section 3, we fix the temperature at 54.15°C and determine ranges for Type II parameters as follows.

Determination of Type II parameters: The average of measured *C. jejuni* pre-scald counts were 10^8 CFU/carcass for the 54.15°C scalding experiment, so we estimate $\sigma = 5 \times 10^7$ CFU/kg (Osiriphun et al., 2012). For *C. jejuni* inactivation in the scald water with pH 8 and temperature $T = 54.15^\circ\text{C}$, using the last equation in (3), we calculate that $I_w(8, 54.15) \in [0.54, 2.82]$ (1/min).

Using methods found in (Osiriphun et al., 2012) and the calculated range for $I_w(8, 54.15)$, we calculate the bacteria shed rate from carcass surfaces k_{cw} and the rate of *C. jejuni* thermal surface inactivation I_c . In particular, we first find $k_{cw} + I_c$ using pre-scald and post-scald experimental counts in (Osiriphun et al., 2012). Next we inform the mass balance found in (Osiriphun et al., 2012) with $I_w(8, 54.15)$ calculated above, processing specifications in Table 1, and scald water counts taken from samples during a 54.15°C scald in (Osiriphun et al., 2012). This allows us to find $k_{cw}/(k_{cw} + I_c)$ and then subsequently ranges for k_{cw} and I_c . Carrying out this process

Table 1
Parameter values and ranges from Section 3.2

Name	Type I parameters	Value/Range	Units
T_V	Scald tank volume	5900	L
g	Water overflow	172	L/min
d_s	Carcass exit rate	1/1.85	1/min
m_c	Typical carcass mass	2	kg
N	Rate of incoming poultry mass	400	kg/min
pH	pH of scald water	8	
T	Temperature of scald water	54.15	$^\circ\text{C}$
Type II parameters			
I_w	Scald water thermal kill rate at pH 8 and 54.15°C	[0.54, 2.82]	1/min
k_{cw}	Carcass to water bacterial shed rate	[0.31, 1.55]	1/min
I_c	Carcass thermal surface kill	[0.74, 1.98]	1/min
σ	Input <i>C. jejuni</i> load	5×10^7	CFU/kg

we find $I_c \in [0.74, 1.98]$ 1/min and $k_{cw} \in [0.31, 1.55]$ 1/min. Notice that the range for I_c as compared with I_w is reasonable as I_w should in general exceed I_c (Osiriphun et al., 2012).

3.3. Transient dynamics

We investigate the transient dynamics of (3) using parameter values/ranges from Table 3.3 (i.e. in the context of pH = 8 and scald water temperature $T = 54.15^\circ\text{C}$). For parameter sampling and simulation details, see the caption in Fig. 3 as well as Appendix C. The results are depicted in Fig. 3 for the first 30 min of a (8 + hour) scalding shift. The system rapidly approaches steady state (within minutes), and as a result, the steady state (4) is an excellent approximation for the model (3) over a working day. A similar transient time may be found analytically by non-dimensionalizing the model (3).

4. Validation of the scald model

We validate model (3) by comparing its prediction of *C. jejuni* levels in the scald water against the experimental data in (Osiriphun et al., 2012) for scald water with pH = 8 and temperature $T = 61.08^\circ\text{C}$. In particular, we use the steady state equation (4) to compare the predicted *C. jejuni* counts in the scald water (W^* at $T = 61.08^\circ\text{C}$) with the measured counts coming from (Osiriphun et al., 2012). The justification for using the steady state equation (4) is as follows: notice that the transient time for the model (3) solutions to reach steady state, in the $T = 54.15^\circ\text{C}$ context, is on the order of minutes (see Fig. 3). In the $T = 61.08^\circ\text{C}$ context, the transient time for the model (3) solutions are even shorter. Recall that the convergence rate of the (3) solutions $v_p(t)$ and $W(t)$ to steady state depends on the magnitude of the parameter combinations $I_w + g/T_V$ and $k_{cw} + I_c + d_s$ respectively. At the higher temperature $T = 61.08^\circ\text{C}$, I_w and I_c increase in magnitude and therefore reduce the transient time. The overflow rate g/T_V and carcass residence time in the scalding tank d_s do not change (Osiriphun et al., 2012). Furthermore, we argue that the range of bacteria shed rate, k_{cw} , determined by the calculations in Section 3.2 at $T = 54.15^\circ\text{C}$, should not change significantly at $T = 61.08^\circ\text{C}$ as this rate depends more on the shear forces in scald water.

The steps for validation of (3) at pH 8 and $T = 61.08^\circ\text{C}$ are as follows: (i) Using the pre/post scald *C. jejuni* counts on carcasses from (Osiriphun et al., 2012) we calculate that $k_{cw} + I_c = 2.28$ (1/min). (ii) Next, because $k_{cw} \in [0.31, 1.55]$ (1/min); we determine that $I_c \in [1.79, 3.03]$ (1/min); (iii) Using these ranges, we calculate v_p^* from (4) and then substitute the resulting values into the equation for W^* from (4). For $k_{cw} = 0.31$, model (3) predicts that $W^* \in [0.15, 74]$ CFU/ml and for $k_{cw} = 1.55$, $W^* \in [0.75, 368]$ CFU/ml. The measured *C. jejuni* count in the scald water from (Osiriphun

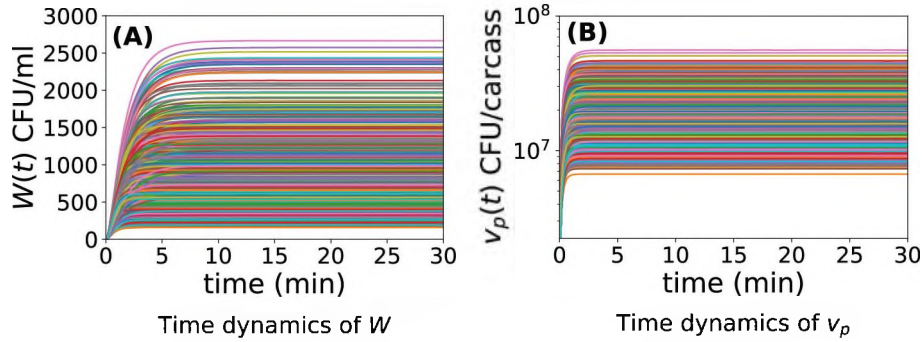


Fig. 3. Transient dynamics of viable *C. jejuni* concentration in scald water (A) and average carcass contamination in the scalding tank v_p (B). Each curve corresponds to a numerical solution of the scald model (3) with a single parameter set taken from ranges in Table 3.3 at 54.15°C. Parameter sets ($n = 1000$) are taken by Latin hypercube sampling (LHS) (for details see (Marino et al., 2008)). We compute solutions numerically with MATLAB. Variation in the rate of convergence to the steady state of $W(t)$ and $v_p(t)$ is a result of parameter sampling. In the case of scald water concentration $W(t)$, this rate is determined by $I_w + \frac{d_s}{k_c}$. Since I_w is sampled from a range, the rate of convergence changes in each solution curve as a result. A slowly responding solution then corresponds to inactivation rate I_w on the low end of its range. Variation is also seen in convergence of average scald carcass levels $v_p(t)$, determined by rate $k_{cw} + I_c + d_s$, i.e., the average rate bacteria leaves compartment v_p .

et al., 2012) was 24.5 CFU/ml, showing good agreement with the predicted W^* ranges from model (3). We expect that the measured bacteria levels should be on the low end of our predicted ranges for W^* as total solids (TS) counts were low (2 mg/ml reported in (Osiriphun et al., 2012) and typical TS counts in the scalding tank are 2–8 mg/ml (Cason et al., 1999)). Hence buffering effects of organic material on *C. jejuni* killing were limited (Yang et al., 2001).

The above validation raises a number of points. In addition to directly justifying the predictive capacity of model (3), it provides additional justification for the inactivation model (1) in scald water. In particular, it supports the notion that a Gaussian relationship (with respect to varying pH) at temperatures other than than $T_{ref} = 52^\circ\text{C}$ is adequate to capture inactivation in scald water. Furthermore, model (3) can aid experimental approaches to explore this claim more rigorously. That is, model (3) can provide a reference point against which to compare experimental results subject to different scalding specifications as well as varying incoming bacteria loads on carcasses. This type of tool is crucial in an industry where experimental data is difficult to synthesize. Finally, we note that the parameter estimation technique outlined in Section 3.2 informed by our inactivation model (Section 2) gives estimates for *C. jejuni* inactivation on carcass surfaces (I_c) during scalding as a function of pH and temperature. Such rates would be difficult to determine directly from experimentation alone.

5. Discussion

5.1. Implications of W^* variation for cross-contamination

The dependence of W^* on the inactivation rate I_w gives insight toward situations for which cross-contamination in the scalding process are most likely. It is reasonable to assume that bacteria attach to carcass surfaces at a rate proportional to the *C. jejuni* concentration in the scald water (Osiriphun et al., 2015). Due to the fact that *C. jejuni* is inactivated more slowly in neutral pH scald water than in acidic or alkaline scald water, cross-contamination becomes more prevalent at neutral pH. While cross-contamination is most prevalent at neutral pH for a given temperature, scald water temperature still plays a pivotal role due to the dependence of W^* on I_w . Note that W^* is essentially inversely proportional to I_w due to the relative size of I_w compared to g/T_V (see scald model steady state equation (4)). We see experimental evidence of this throughout literature. For example, in (Osiriphun et al., 2012) raising temperature from 54.15 °C to 61.08 °C while pH remained constant at 8 resulted in lower viable *C. jejuni*

concentration in scald water (from 794 CFU/ml to 24.5 CFU/ml). Hence the dangers of cross-contamination are highest at neutral pH values and low operating scald temperatures. Additionally, these findings are also in agreement with experimental results in (Lillard et al., 1987).

5.2. Potential risks and side-effects of manipulating scalding pH with additives

Although cross-contamination, bacteria counts, and prevalence at a given operating temperature may be reduced by adjusting the pH of scald water, the risks and effects of additives must be weighed. Carcass skin color, skin quality, ease of feather removal post-scald, poultry plant safety, etc. all depend on scald water pH (Humphrey and Lanning, 1987). Skin color and quality are optimal at pH 8.5 (Humphrey and Lanning, 1987). Feather removal becomes more difficult at pH values above 9.5 (Humphrey and Lanning, 1987). Alkaline additives such as NaOH have caused sickness to workers as a result of the high concentrations of ammonia released (Humphrey and Lanning, 1987). McKee et al. note the possible danger of using alkaline additives in scalding as they could inactivate chlorine in the subsequent chilling process (McKee et al., 2008). Consideration for cost and availability of additives must also be taken into account (Okrend et al.). Thus care must be taken in deciding the best course of action for combating cross-contamination while keeping the risks at a minimum in other regards.

5.3. Application to canadian processors

We demonstrate the applicability of our *C. jejuni* inactivation model using results of an unpublished 2012–2013 processor survey from The Canadian Poultry and Egg Processors Council. Scald water temperature and pH is given in Table 2 for seven industrial plants in Canada. Alongside the processing data, we include ranges for *C. jejuni* killing rate $I_w(pH, T)$ for the scalding configuration. There is high variation for inactivation $I_w(pH, T)$ across the seven plants. Note plants A,D,G likely use chemical additives as their pH is extreme relative to tap water. Plants A, D, G also have far higher inactivation rates as they avoid the pH 7 danger zone where thermal resistance is maximum (Humphrey and Lanning, 1987; Okrend et al.; Bazin and Prosser, 1988). Plants A and B implement a cost-effective strategy in using the first scalding tank to merely remove organic material from birds, then subsequent high temperature scald to rapidly inactivate bacteria (see Table 3).

We provide a simple illustrative example showing the application

Table 2
Parameter values and ranges from Section 4 used for model validation.

Name	Type I parameters	Value/Range	Units
T_V	Scald tank volume	5900	L
g	Water overflow	172	L/min
d_s	Carcass exit rate	1/1.85	1/min
m_c	Typical carcass mass	2	kg
N	Rate of incoming poultry mass	400	kg/min
pH	pH of scald water	8	
T	Temperature of scald water	61.08	°C
Type II parameters			
I_w	Scald water thermal kill rate at pH 8 and 61.08 °C	[3.30,1628.95]	1/min
k_{cw}	Carcass to water bacterial shed rate	[0.31,1.55]	1/min
I_c	Carcass thermal surface kill at pH 8 and 61.08 °C	[1.79, 3.03]	1/min
σ	Input <i>C. jejuni</i> load	4.5×10^7	CFU/kg

Table 3
Scalding temperature and pH information from a survey of industrial poultry plants in Canada taken between December 1, 2012 and December 31, 2013.

Plant	Temperature in °C (pH) [Range on I_w]	Scald tank 2	Scald tank 3
	Scald tank 1		
A	51.67 (9) [≈ 1]	53.33 (9) [1.3, 6.2]	58.89 (9) [5.6, 1017.5]
B	34 (7.83) [≈ 0]	60 (7.83) [2.2, 509.3]	
C	58.5 (7) [1.1, 80.8]		
D	58.33 (5) [3.3, 289.9]		
E	58.3 (7) [1.0, 67.3]		
F	61.1 (6.7) [2.2, 864.8]		
G	58.3–58.89 (4) [18, 3841.2]		

of inactivation model $I_w(pH, T)$. With the link between temperature and pH, we provide alternatives to several of the Canadian poultry plants in Table 2. Primary items to consider regarding cost-effective scalding are energy prices for heating scald water and prices of chemical additives. As a result, plant-specific control problems of maximizing of $I_w(pH, T)$ while minimizing costs may be posed.

Plant A maintains high pH in all three tanks through use of additives. However, in the first stage we see low inactivation rates $I_w(pH, T)$. A low kill rate combined with a high amount of organic material typically seen in the first stage (details in (Cason et al., 1999)) will result in buffering an already low inactivation rate. It may be more effective to discontinue use of additives in tank 1, keeping the pH high in tanks 2 and 3. After all, the vast majority of inactivation takes place in the hotter, latter stages with little buffering effects from organic material. The increased pH in the high temperature tanks take advantage of the synergistic effect, that is, the combination of extreme pH environment and high temperature (McKee et al., 2008). Plant B may benefit from a similar strategy.

Plants E and F conduct scalding at high temperature at a neutral pH. While plants E and F maintain a high inactivation rate, we provide two alternatives which may improve end-result microbiological quality and also prove cost-effective. For example, plant E could maintain a similar inactivation rate using additives while operating at a lower temperature. For instance, consider pH 9.3 together with a (lower) temperature of 55.3 °C ($I_w(9.3, 55.3) \in [3.5, 71.4]$) and pH 4 at 54.5 °C ($I_w(4, 54.5) \in [6, 68.4]$). Thus the increase of the lower bound inactivation rate and lower scald temperature may result in a higher quality end product as the epidermis is removed in high temperature scalding. For plant F we may suggest lowering the temperature slightly and maintaining an acidic or alkaline pH environment. To maintain a similar kill rate, plant F may consider pH 9.3 at 58 °C ($I_w(9.3, 58) \in [7, 850.7]$) or pH 4.1 at 57.5 °C ($I_w(4.1, 57.5) \in [10.9, 837.6]$). Again, notice the lower bound on inactivation increases significantly while keeping a similar upper bound. Lowering the temperature while maintaining pH in a reasonable range may result in a higher quality skin appearance while being cost-effective.

5.4. Conclusions and future directions

The foundational papers of Lillard et al. (1987), Okrend et al. Okrend et al., Humphrey and Lanning (1987) are summarized in Section AppendixA. These works all note that cross-contamination may be reduced by introducing acidic or alkaline additives to scald water. While our findings are in agreement with these works, it is important to note that our work expands on this idea. In particular, we quantify how the bacteria level in the scald water W is linked to pH and temperature via model (3). While pH is certainly important, we illustrate how the temperature, pH pair determines the *C. jejuni* kill rate in scald water. As the magnitude of W is directly related to cross-contamination, in effect, our model (3) provides a quantifiable connection between the temperature, pH pair and potential for cross-contamination.

In terms of control, this quantitative link (via $I_w(pH, T)$) is applicable in a HACCP context, suggesting that the pH - temperature pair is a critical control parameter in the scalding stage. Previous works have experimentally verified the thermal resistance of *C. jejuni* and other heat-sensitive bacteria to be highest in a neutral pH environment (Humphrey and Lanning, 1987; Okrend et al.). USDA best practice recommendations suggest maintaining scald water pH below 6.5 or above 7.5 (Bennett, 2008). Our work may be used to further inform these recommendations as model (3) quantifies the synergistic role temperature and pH play in *C. jejuni* inactivation, especially in light of given performance standards or maximum acceptable pathogen levels. As demonstrated in Section 4, model (3) adequately captures the mechanisms involved with *C. jejuni* kill rates in scald water. Note that some inactivation models, developed for different types of bacteria in media differing from that of scald water, have employed terms to further specify the pH-temperature effect on inactivation (Cerf et al., 1996; Gaillard et al., 1998). With detailed scalding experiments, quantifying *C. jejuni* D-values relative to multiple pH-temperature pairs, it would be important to see if increased model complexity is necessary in the scalding context. Armed with such predictive confidence, the implementation of model (3) (or model (3) with an augmented inactivation term) into quantitative microbial risk

assessment (QMRA) models, may also give insights into new risk-management strategies, and provide valuable information for policy-making.

In terms of pre-scald contamination, the model (3) considers a fixed, average rate of incoming bacteria on all carcasses σ . Realistically there is variation in the incoming bacteria levels on each bird (FAO/WHO, 2009). An individual-based model could take into account experimental flock prevalence and counts by varying σ in time. It is then possible to quantify the spread of highly contaminated birds to their neighbors. Our model (3), parameter estimation, and thermal inactivation bounds on $I_w(pH, T)$ may inform such an individual-based model.

Further investigation of the impact of solids and organic material concentrations present in scald water on inactivation rates could give a clearer picture of bacteria inactivation in scalding. We propose that an experiment determining *C. jejuni* D-values in the presence of varying organic material concentrations relevant to scalding, similar to that in (Yang et al., 2001), would be significant. The typical concentrations of organic material in scalding water are 2–8 mg/ml (Cason et al., 1999). With this experimental information, data fitting and inactivation model construction techniques presented in Section 2 may be utilized to leverage these findings.

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Appendix A. Review: experiments using additives

Appendix A.1 pH influence on carcass and scalding water microbiological quality

We present a review of key experiments which study the effects of scald water pH on microbiological quality at the scalding stage. Experiments in (Humphrey and Lanning, 1987) and (Berrang et al., 2011) compare high pH (alkaline) scalding to the natural pH which tends to be neutral. On the other hand, (Okrend et al.) and (Lillard et al., 1987) compare low pH (acidic) scalding to a typical neutral pH control. Scald water pH is modified via additives such as calcium hydroxide (alkaline), sodium hydroxide (alkaline), acetic acid (acidic), and more recently peracetic acid (acidic). Scald water bacteria concentrations and prevalence are significantly reduced in (Humphrey and Lanning, 1987) within the high pH group. Significant reduction in carcass sample prevalence and concentrations are also seen in (Humphrey and Lanning, 1987) and (Berrang et al., 2011). The interested reader is invited to see the details in below in Section Appendix A.2, which include experimental procedures, bacteria counts, and prevalence.

Appendix A.2 Review: scald water pH influence in scalding

Humphrey and Lanning (1987), Berrang et al. (2011), compare pre-scald and post-scald *Campylobacter* prevalence on carcasses sent through scald tanks operating at (i) high pH and (ii) conventional (control) pH. Berrang et al. raise the pH of scald water through the addition of calcium hydroxide ($\text{Ca}(\text{OH})_2$) while Humphrey and Lanning raise scald water pH with sodium hydroxide (NaOH). Berrang et al. find a significant reduction in *Campylobacter* positive carcass prevalence (%) and also mean concentration in rinse samples (log CFU/ml) in a high pH scald (mean pH 9.89) compared to control scald (mean pH 6.88). Pre-scald carcass prevalence of control and high pH

groups were both 90%, while post-scald prevalence of the control and high pH groups were 57% and 17%, respectively. Pre-scald carcass rinse samples of both control and high pH groups contained 3.28 logCFU/ml, whereas control and high pH groups contained 1.15 and 0.44 logCFU/ml after scalding, respectively. Similar results were reported by Humphrey and Lanning. In Berrang et al., scald water in control group had mean pH 6.4 and high pH group scald water had mean pH 9.18. A 60% reduction of *C. jejuni* positive skin samples was observed. Hence we see a significant reduction of carcass contamination and prevalence by changing only scald water operating pH. Humphrey and Lanning also compared *C. jejuni* prevalence and most probable number (MPN) in scald water for both control and high pH scald water. 12 of the 15 scald water samples in the control group were *C. jejuni* positive. On the other hand, 4 of the 15 high pH scald water samples were *C. jejuni* positive. Reduction in *C. jejuni* MPN from 82.3/100 ml (823 MPN/ml) to 1.5/100 ml (15 MPN/ml) was reported in control and high pH scald water samples. Hence we see that the addition of NaOH reduced MPN and prevalence significantly – an artifact of inactivation rates increasing as pH moves away from neutral.

On the acidic side of the pH spectrum, Okrend et al. (Okrend et al.) and Lillard et al. (1987), experiment with acetic acid as a scalding additive and in particular its impact on microbiological quality of scald water and carcass surfaces. Lillard et al. measure *Salmonellae*, *Enterobacteriaceae*, and total aerobic bacteria in additive-free scald water (control pH 6.9) and also with 0.5% acetic acid (pH 3.6). Post-scald (unpicked) bacteria quantity for control and acetic acid treated groups are also provided. In contrast to the studies of Berrang et al. and Humphrey and Lanning, the carcass surface aerobic bacteria count, *Enterobacteriaceae* count, and *Salmonellae* prevalence (%) all fail to reduce significantly with the use of 0.5% acetic acid. On the other hand, total aerobic bacteria and *Enterobacteriaceae* were reduced significantly in scald water by the presence of 0.5% acetic acid in the treatment group. None of the scald water samples were *Salmonellae* positive in both control and acetic acid treated groups. Lillard et al. note bacteria are protected by feathers, fecal matter, and skin in such a way that buffered acetic acid's effect on inactivation rate. Lillard concludes by noting the use of acetic acid for controlling cross-contamination in scalding due to the decrease in pathogens in scald water, but not to reduce carcass surface contamination. Note this is in contrast to the findings of Berrang et al., Humphrey and Lanning, who find significant reductions in surface contamination. Okrend et al. experimentally determine D-values of *C. jejuni* in untreated scald water (pH 6.97) and scald water treated with 0.1% acetic acid (pH 4.38). Untreated scald water yielded a D-value of 5.97 min while 0.1% acetic acid treated scald water yielded a lower D-value of 1.20 min.

Appendix B. Supplementary material to section 2

Appendix B.1. Fixed-pH, temperature varying experiments

Campylobacter jejuni decimal reduction times at varying temperatures are found in the papers of Sakkaf and Jones (Al Sakkaf and Jones, 2012), Doyle and Roman (1982), Sorqvist (Sorqvist, 1989), Blankenship and Craven (1982), Waterman (1982), and Nguyen et al. (2006). In total there are D-values provided for 17 *C. jejuni* strains across these six works and are displayed graphically in Fig. 1A. While heating menstruum (and therefore pH) change between papers, the heating menstruum remains constant within each paper's experiments. Even so, we see vast differences in the reports of decimal reduction times for *C. jejuni* with respect to temperature across these six papers. We see a high variation in kill rates especially in the lower temperature ranges; as temperature increases this variation appears to decrease. Doyle and Roman report D-values of 3.5–5.1 min at 50°C for all five *C. jejuni*

strains in their experiments Doyle and Roman (1982). On the other hand, Nguyen et al. report D-values of 36–39 min with 2 strains of *C. jejuni* at 50 °C (Nguyen et al., 2006). These near ten-fold differences could be attributed to Doyle and Roman using skim milk (pH 6.8) as heating menstruum and Nguyen et al. using heart infusion broth (pH 7.4) (Nguyen et al., 2006; Doyle and Roman, 1982). In other words, strain heat sensitivity, experimental method, and variables such as heating menstruum may greatly impact the inactivation of *C. jejuni*. However we see that Doyle and Roman, Blankenship and Craven, Waterman, and Sorqvist all report tight D-value ranges over the relevant scalding temperature spectrum (Waterman, 1982; Sorqvist, 1989; Blankenship and Craven, 1982; Doyle and Roman, 1982). For example, at 55 °C all such D-values found by Doyle and Roman, Blankenship and Craven, Waterman, and Sorqvist were between 0.47 and 1.14 min despite slightly different experimental methods and heating menstruum (Waterman, 1982; Sorqvist, 1989; Blankenship and Craven, 1982; Doyle and Roman, 1982).

Appendix B.2 Fixed-temperature, varying pH experiments

Humphrey and Lanning had taken scald water samples at the end of a working day from a scald tank and used these samples as heating menstruum to experimentally determine *C. jejuni* D-values at 52 °C (Humphrey and Lanning, 1987). The scald water samples contained 13 mg/ml total solids and 6.2 mg/ml proteins. To quantify the impact of pH on *C. jejuni* kill rate, varying levels of sodium hydroxide (NaOH) and hydrogen chloride (HCl) were used to control the pH of the scald water samples (Humphrey and Lanning, 1987). In particular, Humphrey and Lanning find D-values at constant temperature 52 °C and pH values of 4, 6, 7, 8, 9, and 10 to be 0.4±0.02 min, 8.72±0.12 min, 11.50±0.2 min, 6.40±0.28 min, 2.00±0.41 min, 1.00±0.22 min respectively (Humphrey and Lanning, 1987).

Appendix B.3 Parameter estimation for model (1)

Recall the form of the inactivation model (1) is given by: $D_{w_i}(pH, T) = D(pH)|D_i(T)|$, where $D_i(pH) = \hat{a}e^{-(pH-b/c)^2}$ and $D_i(T) = a_i e^{b_i(T-T_{ref})}$. The following provides details concerning parameter estimates, using MATLAB's 'cftool' for the model forms with respect to pH and temperature.

To estimate parameters for $D(pH)$, the fixed-temperature *C. jejuni* D-value data from (Humphrey and Lanning, 1987) is used to construct a 95% confidence interval (CI). For each pH sample mean (\bar{x}), D-values are reported with their associated standard error (Humphrey and Lanning, 1987). We obtain the upper bound on the 95% CI by fitting the points $\bar{x} + 1.96 \cdot SE$ to a Gaussian $D_U(pH)$. Data fitting yields coefficients a_U, b_U, c_U for $D_U(pH) = a_U e^{-(pH-b_U/c_U)^2}$. Similarly, a lower 95% CI bound is obtained by fitting $\bar{x} - 1.96 \cdot SE$ to $D_L(pH) = a_L e^{-(pH-b_L/c_L)^2}$ (see Fig. 1B). The data fitting results, along with the respective 95% CI given as an open interval, are $a_U = 11.62$ (9.60, 13.63), $b_U = 6.86$ (6.57, 7.15), $c_U = 1.72$ (1.28, 2.16) and $a_L = 11.3$ (10.5, 12.1), $b_L = 6.80$ (6.70, 6.89), $c_L = 1.49$ (1.33, 1.64).

For $D_i(T)$, we use an exponential thermal inactivation model as outlined in (Bazin and Prosser, 1988) with data fitting to the D-value vs. temperature data. The D-values for 17 strains of *C. jejuni* (coming from (Al Sakkaf and Jones, 2012; Doyle and Roman, 1982; Sorqvist, 1989; Blankenship and Craven, 1982; Waterman, 1982; Nguyen et al., 2006)) are each fit to exponential functions $D_i(T) = a_i e^{b_i(T-T_{ref})}$, where $T_{ref} = 52$ °C. Notice that since the D-value vs. pH experiments (Humphrey and Lanning, 1987), used to determine $D(pH)$, take place in actual scald water at 52 °C with high concentrations of organic material and proteins, we set $T_{ref} = 52$ °C. In addition, we only retain the decay information for each strain given by b_i and reset the estimated a_i to be 1. See Table B.4 for fitting results

(note that we only report the b values and respective CI relative to each strain). The reasoning here is that we rescale the $D_i(T)$ equation so that $D_L(pH) \leq D_{w_i}(pH, T_{ref}) \leq D_U(pH)$. Note that, by setting $a_i = 1$ and $T_{ref} = 52$ °C, we impose the condition that model (1) determined D-values agree with the cross-section illustrated in Fig. 1B. In effect, this allows us to have an inactivation model in the water that is linked as close as possible to data from industrial scalding.

Table B.4

Results of parameter estimation for decay rates of $D(T)$ relative to *C. jejuni* strain

Strain	b	95% CI	Reference
AR6	-0.38	(-0.42, -0.35)	(Nguyen et al., 2006)
L51	-0.43	(-0.56, -0.29)	
CF3	-0.42	(-0.43, -0.39)	(Doyle and Roman, 1982)
CF6	-0.26	(-0.36, -0.16)	
CF8	-0.32	(-0.50, -0.15)	
CF12	-0.48	(-0.71, -0.25)	
CF16	-0.39	(-0.48, -0.30)	
5388	-0.61	(-0.99, -0.23)	(Waterman, 1982)
21033	-0.92	(-2.22, 0.38)	
16000	-0.57	(-1.32, 0.19)	
16509	-0.61	(-1.36, 0.13)	
17259	-0.62	(-2.85, 1.61)	
24791	-0.38	(-2.01, 1.24)	
1503	-0.54	(-1.37, 0.28)	(Sorqvist, 1989)
ST45	-0.66	(-0.73, -0.59)	(Al Sakkaf and Jones, 2012)
ST190	-0.54	(-0.58, -0.49)	
ST474	-0.56	(-0.82, -0.30)	

To account for all experimental variation in temperature decay, we allow $D_w(pH, T)$ to vary between D_{w_i} for all *C. jejuni* strains i . Naturally, there are lower and upper bounding D_{w_i} for which the lowest and highest D-values are seen. By allowing D_w to vary between these lower and upper bounds, we retrieve our inactivation model which addresses items 1), 2), and 3) proposed in Section 2.2. Among the 17 *C. jejuni* strains, we find the steepest temperature decay in Waterman's strain 21033 ($b_{21033} = -0.92$). On the other hand, the *C. jejuni* strain with the most mild temperature decay is strain CF6 found in $b_{CF6} = -0.26$ Doyle and Roman (1982). Finally, we obtain the inactivation model

$$\begin{cases} D_{L_{CF6}} \leq D_w \leq D_{U_{21033}} & T \leq 52^\circ \text{C} \\ D_{L_{21033}} \leq D_w \leq D_{U_{CF6}} & T \geq 52^\circ \text{C}. \end{cases} \quad (\text{B.1})$$

Appendix C. Generating solutions to model (3) as illustrated in Fig. 3

We outline the procedure for producing a single curve in Fig. 3. The idea is to take random samples from the provided ranges in Table 1 at 54.15 °C to completely determine scald model (3) parameters. In other words, we aim to provide single values for k_{cw} , l_c , and l_w . Sampling from the uniform distribution $U(0, 1)$, we may then generate corresponding parameter values. For example, shed rate k_{cw} lies between 0.31 and 1.55 1/min, we generate a value in this interval using the following transformation $k_{cw} = 0.31 + r_1(1.55 - 0.31)$ where r_1 is a random sample from $U(0, 1)$. In the case of Figure AppendixC we generate $r_1 = 0.65$ and as a result $k_{cw} = 1.11$ 1/min. Similarly, for the carcass inactivation rate l_c and the water inactivation rate l_w , sampling from $U(0, 1)$ to obtain $r_2 = 0.39$ and $r_3 = 0.75$, then plugging the respective values into $l_c = 0.74 + r_2(1.98 - 0.74)$ and $l_w = 0.54 + r_3(2.82 - 0.54)$, we determine $l_c = 1.54$ 1/min and $l_w = 2.01$ 1/min. In general, a sample for parameter p which varies from p_{min} to p_{max} may be generated by computing $p = p_{min} + U(0, 1)(p_{max} - p_{min})$.

The curves in Figure AppendixC are produced using MATLAB's ODE45 to solve the scald model (3) with the values for k_{cw} , I_c , and I_w found above as well as fixed values found in Table 1. The method for generating $n = 1000$ curves in Fig. 3 is similar.

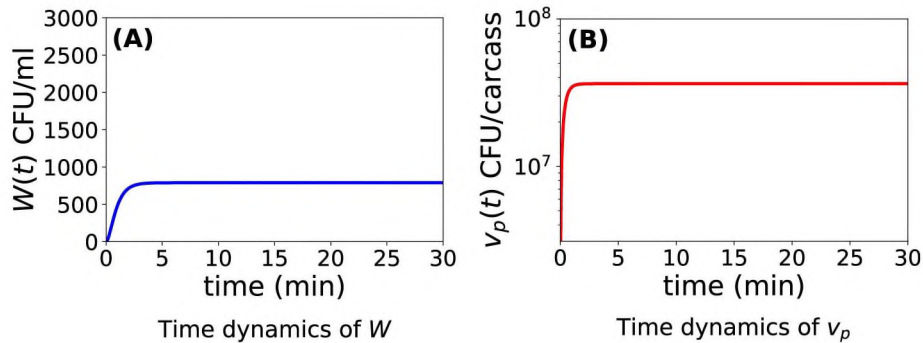


Figure C.4. Solutions to scald model (3) run at 54.15 °C corresponding to a single parameter set; shed rate $k_{cw} = 1.11$ 1/min, carcass inactivation rate $I_c = 1.54$ 1/min scald water inactivation rate $I_w = 2.01$ 1/min, and fixed parameter values found in Table 1. We illustrate the method for finding k_{cw} , I_c and I_w in AppendixC. Solutions to scald model (3) are found numerically using MATLAB's ODE45 using initial conditions $v_p(0) = 0$, $W(0) = 0$.

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