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Relationship Between Jump Landing Kinematics and Peak ACL Force During a Jump in Downhill Skiing: A Simulation Study

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Original Citation
Recent data highlight that competitive skiers face a high risk of injuries especially during off-balance jump landing maneuvers in downhill skiing. The purpose of the present study was to develop a musculo-skeletal modeling and simulation approach to investigate the cause-and-effect relationship between a perturbed landing position, i.e., joint angles and trunk orientation, and the peak force in the anterior cruciate ligament (ACL) during jump landing. A two-dimensional musculo-skeletal model was developed and a baseline simulation was obtained reproducing measurement data of a reference landing movement. Based on the baseline simulation, a series of perturbed landing simulations \( (n = 1000) \) was generated.

Multiple linear regression was performed to determine a relationship between peak ACL force and the perturbed landing posture. Increased backward lean, hip flexion, knee extension, and ankle dorsiflexion as well as an asymmetric position were related to higher peak ACL forces during jump landing. The orientation of the trunk of the skier was identified as the most important predictor accounting for 60% of the variance of the peak ACL force in the simulations. Teaching of tactical decisions and the inclusion of exercise regimens in ACL injury prevention programs to improve trunk control during landing motions in downhill skiing was concluded.
analyzed modifications in initial hip and knee flexion, hip internal rotation, and hip internal rotation velocity on knee joint loading in a series of side-step cutting simulations. In the simulation study of Gerritsen et al. (1996), a possible injury situation was investigated during jump landing in downhill skiing. A single backward off-balance landing movement in combination with an active recovery movement was simulated and the peak force in the ACL was predicted. However, up to now, there is a lack of simulation studies focusing on a systematic analysis of the relationship between the kinematics of the skier prior to ground contact and the subsequent peak ACL force during jump landing in downhill skiing.

The purpose of the present study was to develop a musculo-skeletal modeling and simulation approach to investigate the effect of a perturbed landing position, i.e., joint angles and trunk orientation, on peak ACL force during the subsequent landing movement.

**Methods**

Musculo-skeletal model

A planar, musculo-skeletal model of an alpine skier with two skis was developed. The skier model consisted of seven rigid segments, one segment representing the head, arms and torso, and three segments for each lower extremity: thigh, shank, and one segment for the foot and the ski boot. The restraining component of the ski boot was represented as passive joint moment acting at the ankle joint (Gerritsen et al., 1996). The model of each ski consisted of a chain of nine rigid segments connected by revolute joints. Bending stiffness and damping properties of the skis were integrated into the model using linear spring-damper elements attached to the revolute joints. Parameters of the spring-damper elements were derived from bending experiments and ski vibration tests (Bruck et al., 2003) of a downhill ski with a nominal length of 2.11 m. Multibody dynamics was derived based on Kane’s method using Autoolev 4.1 (Symbolic Dynamics Inc., Sunnyvale, California, USA). In total, the skier-ski system had 25 kinematic degrees of freedom and the equations of motion were formulated as:

\[
M(q) \ddot{q} + B(q, \dot{q}) + R(q)F_M = 0
\]  

where \(q\), \(\dot{q}\), and \(\ddot{q}\) are the generalized coordinates, velocities, and accelerations; \(M(q)\) is the system mass matrix; \(B(q, \dot{q})\) is a vector of generalized forces due to gravity, external forces and moments, coriolis and centrifugal forces and moments, and passive joint moments; \(R(q)\) is a matrix of muscle moment arms; \(F_M\) is a vector of muscle forces and \(R(q)F_M\) is a vector of net joint moments.

The motion of the skier was actuated by 16 muscles, eight for each lower extremity: iliopsoas (II), glutei (Gl), hamstrings (Ham), rectus femoris (RF), vasti (Vas), gastrocnemius (Gas), soleus (Sol), and tibialis anterior (TA). Each muscle was modeled as a three-element Hill-type model. Contraction dynamics incorporating the force-length-velocity properties of the muscle was modeled as function of muscle fiber length, \(L_{CE}\), fiber lengthening velocity, \(\dot{L}_{CE}\), activation, \(a\), and muscle length, \(L_d(q)\) (McLean et al., 2003),

\[
g(L_{CE}, \dot{L}_{CE}, a, L_d(q)) = 0
\]  

Activation dynamics was modeled as a first-order process (He et al., 1991):

\[
h(a, \dot{a}, u) = 0
\]  

where \(u\) denotes the neural excitation of the muscles. A linear relationship was assumed between joint angles and muscle-tendon length (McLean et al., 2003) and muscle parameters were taken from Gerritsen et al. (1996). In total, the musculo-skeletal model of the skier and the two skis had 82 state variables \(x = [q, \dot{q}, a, L_{CE}]^T\) and 16 control variables \(u\). The dynamics of the skier-ski model was given by eqns. [1], [2], and [3].

Contact models

Contact between skis and snow was modeled by two types of forces applied at the mass center of each ski segment: a penetration force, \(F_p\), acting normal to the snow surface and a friction force, \(F_f\), acting parallel to the snow surface. The penetration force was given by the following equation:

\[
F_p = k_p A \left( \frac{1}{2} d + \frac{1}{2} \sqrt{d^2 + d_p^2} \right) (1 + b_d d) \quad [4]
\]

where \(d\) and \( \dot{d} \) are the penetration depth and velocity of the segment’s center of mass, \(A\) is the area of the rectangularly approximated base of the segment, and \(k_p\) and \(b_p\) are ski-snow contact parameters. The stiffness parameter \(k_p\) was set to \(6 \times 10^5\) N/m to get a maximum penetration of about 0.05 m at the ski below the area of the ski boot. In reality, the penetration below the area of the ski boot corresponds to the deformation of the heel pad, the liner of the ski boot, the ski bindings, and the snow. The damping parameter \(b_p\) was set to 0.75 s/m. The parameter \(d_p\) represents a smooth transition region of the contact model and was set to 0.01 m. The friction force \(F_f\) was approximated by Coulomb friction with a friction coefficient of \(\mu = 0.1\) (Kaps et al., 1996):

\[
F_f = -\mu F_p \frac{v}{\sqrt{v^2 + v_0^2}} \quad [5]
\]

where \(v\) denotes the sliding velocity parallel to the snow surface. The smoothing parameter \(v_0\) was set to 1 m/s. Air drag was applied on each segment of the skier based on the regression model of Barelle et al. (2004), which describes the relationship between total drag force and the skier’s body size and posture.

Baseline simulation of landing movement

A baseline simulation was obtained in which muscle stimulation patterns of the model were optimized to track a reference landing movement in competitive downhill skiing. In particular, the following optimal control problem was solved, minimizing the cost function:

\[
J = J_1 + J_2 + J_3
\]

with

\[
J_1 = \frac{1}{N_T \sigma} \sum_{i=1}^{N_T} \left( \frac{q_i(t) - q_i^{set}(t)}{\sigma_i} \right)^2 dt \quad [7]
\]

\[
J_2 = \frac{w_{\text{mus}}}{N_T} \sum_{i=1}^{N_T} u_i(t)^2 dt \quad [8]
\]

and

\[
J_3 = \frac{w_{\text{a}}}{2N_T} \sum_{i=1}^{N_T} \sum_{i=1}^{N_a} \left( q_i(t)^2 + \dot{q}_i(t)^2 \right) dt \quad [9]
\]

subjected to constraints because of the dynamics of the skier-ski model and upper and lower bounds on the controls \(0 \leq u \leq 1\).
perturbed landing position. With the initial posture of the skier was chosen to avoid that the ski tails penetrate the snow in the distorted landing position prior to ground contact on peak ACL force reached 695 N after 33 ms of ground contact; in the left knee, peak ACL force amounted to 165 N (Fig. 3). In the Monte Carlo simulations (n = 1000), substantially higher peak ACL forces were observed compared with the baseline simulation (Fig. 4) reaching values up to 2017 N.

The multiple regression analysis showed that the posture variables of the skier prior to ground contact significantly predicted the peak force in the ACL during the subsequent landing movement \[ F(7,951) = 956.34, \]
In the regression model, the orientation of the trunk, the joint angles at the hip, knee and ankle of the loaded lower extremity, and the difference in hip and knee flexion were included (Table 1) accounting for 88% of the variance of the peak force in the ACL. Although the bivariate correlations (Table 2) showed significant relations between each independent variable and the dependent variable, the difference in ankle dorsiflexion did not contribute significantly to the regression.

The individual regression coefficients revealed that increased backward lean, hip flexion, knee extension, and ankle dorsiflexion were related to higher peak ACL forces during the subsequent landing movement. Differences in hip and knee flexion angles, which account for
an asymmetric position, were also related to increased peak ACL forces (Table 2).

The orientation of the trunk of the skier was identified as the most important predictor in the regression model. As indicated by the squared semipartial correlations, 60% of the variance of the peak force in the ACL could be uniquely attributed to the orientation of the trunk segment prior to ground contact (Table 3).

**Discussion**

The purpose of the present study was to develop a musculo-skeletal modeling and simulation approach to investigate the effect of a perturbed landing position, i.e., joint angles and trunk orientation, on peak ACL force during the subsequent landing movement.

A biped musculo-skeletal model of a skier was developed and a baseline simulation was successfully obtained in which muscle stimulation patterns of the modeled skier were optimized to track measurement data of a reference landing movement in competitive downhill skiing. During the baseline simulation, the peak tensile force in the ACL amounted to 695 N (0.9 body weight (BW)) and occurred about 30 ms after initial ground contact. There is a lack of studies reporting ligament forces during a well-performed jump landing in downhill skiing. In the simulation study of Gerritsen et al. (1996), peak ACL force was reported only for a perturbed off-balance situation and amounted to 1350 N; for the unperturbed simulation, only the net knee reaction force was reported. However, durations of 20–40 ms and magnitudes of up to 0.4 BW were reported in

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**Table 1.** Results of the multiple linear regression analysis showing the unstandardized coefficients $B$ and standardized coefficients $\beta$ of the predictor variables. In the multiple linear regression analysis, the peak force in the ACL in the left/right lower extremity during the landing movement was chosen as dependent variable and perturbed kinematic state variables of the posture of the skier prior to ground contact as the predictor variables. The perturbed kinematic state variables were the orientation of the trunk segment, the joint angles at the hip, knee, and ankle of the lower extremity corresponding to the peak force in the ACL as well as the difference in the joint angles at the hip, knee, and ankle of both lower extremities.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$B$</th>
<th>$\beta$</th>
<th>$P$-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trunk orientation (deg)</td>
<td>2902</td>
<td>0.809</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Hip flexion (deg)</td>
<td>2066</td>
<td>0.625</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Knee flexion (deg)</td>
<td>-1069</td>
<td>-0.284</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Ankle dorsiflexion (deg)</td>
<td>257</td>
<td>0.043</td>
<td>0.011</td>
</tr>
<tr>
<td>Hip flexion diff (deg)</td>
<td>1280</td>
<td>0.564</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Knee flexion diff (deg)</td>
<td>-428</td>
<td>-0.169</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Ankle dorsiflexion diff</td>
<td>36</td>
<td>-0.008</td>
<td>0.628</td>
</tr>
</tbody>
</table>

**Table 2.** Bivariate correlations $r$ between the peak ACL force and each of the predictor variables.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$r$</th>
<th>$P$-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trunk orientation</td>
<td>0.787</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Hip flexion</td>
<td>0.166</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Knee flexion</td>
<td>-0.275</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Ankle dorsiflexion</td>
<td>0.260</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Hip flexion diff</td>
<td>0.138</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Knee flexion diff</td>
<td>0.181</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Ankle dorsiflexion diff</td>
<td>-0.274</td>
<td>&lt;0.001</td>
</tr>
</tbody>
</table>

**Table 3.** Semipartial correlations $sr$ for the predictor variables.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$sr$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trunk orientation</td>
<td>0.777</td>
</tr>
<tr>
<td>Hip flexion</td>
<td>0.426</td>
</tr>
<tr>
<td>Knee flexion</td>
<td>-0.199</td>
</tr>
<tr>
<td>Ankle dorsiflexion</td>
<td>0.029</td>
</tr>
<tr>
<td>Hip flexion diff</td>
<td>0.388</td>
</tr>
<tr>
<td>Knee flexion diff</td>
<td>-0.117</td>
</tr>
<tr>
<td>Ankle dorsiflexion diff</td>
<td>0.006</td>
</tr>
</tbody>
</table>
previous studies analyzing drop jumps from a 60 cm platform (Pflum et al., 2004; Kernozek & Ragan, 2008). The considerably higher peak ACL force in the present study might be primarily due to the effective fall height of about 90 cm. The higher fall height is likely to cause an increased tibiofemoral compression force, which would directly elevate anterior tibial load and consequently ACL load due to the tibial plateau angle (Yeow et al., 2010). Additionally, the low friction between skis and snow reduces the posterior ground reaction force, which is considered to protect the ACL.

The simulation with random perturbations of the orientation of the trunk and the joint angles of the skier prior to ground contact resulted in substantially higher peak ACL forces compared with the baseline simulation. Peak ACL forces reached values up to 2017 N. As the ACL typically tears at loads greater than 2000 N (Woo et al., 1991), this peak ACL force might have resulted in a possible injury situation. In the simulation study of Kietlinski & Rzymkowski (2005), also, a high injury risk was reported during a backward off-balance jump landing movement. A peak elongation of the ACL of 20% was predicted and based on the Abbreviated Injury Scale, a high risk of total rupture was concluded. Based on the study of Kietlinski & Rzymkowski (2005) and the results of the present simulations, a sagittal plane ACL injury mechanism might exist during jump landing in downhill skiing. Although the current opinion states that it is highly probable that ACL injuries occur during multi-planar mechanisms of injury (Quatman et al., 2010), a single-planar mechanism might be sufficient to tear the ACL during jump landing in downhill skiing.

Multiple regression analysis revealed that the increase of backward lean, hip flexion, knee extension, and ankle dorsiflexion were related to higher peak ACL forces during the subsequent landing movement. These results are in agreement with video sequences of injury cases during landing movements in world cup downhill skiing. Skiers’ mistakes such as a poor jumping technique and incorrect tactical decisions have been determined as key factors contributing to injury and these mistakes have been observed to result in a backward off-balance situation of the skier during the flight and in landing on the tails of the skis with nearly extended knees (Bere et al., 2011a). Also, in the computer simulation study of Gerritsen et al. (1996), a perturbed backward off-balance landing movement of an alpine skier resulted in higher ligament forces compared with an unperturbed landing simulation. In other sports, more backward lean and an increased distance between the center of mass and the base of support were identified in ACL injuries cases by videotape analysis (Sheehan et al., 2012). Interestingly, our simulation results are consistent with the results of Sheehan et al. (2012), as backward lean in combination with an increase of hip flexion and knee extension results in an increased distance between the center of mass and the base of support.

The orientation of the trunk prior to landing was identified as the most important predictor for high ACL forces among the perturbed variables. This result reveals a set of preventive measures, which could be easily implemented in training and competitions. To keep the trunk in a forward oriented position during jumping skiers have to rotate their body forward during takeoff and stay in a tuck position during flight. Low speed and a gentle change of the radius of the takeoff area ease the necessary forward rotation of the skier to achieve the required angular momentum. Additionally, a straight and sufficiently long inrun favors a proper preparation of the skiers before takeoff. High flight trajectories are likely to result in a more upright orientation of the trunk during flight and landing. Resulting air resistance may act above the center of mass rotating the skier backward especially when the skier’s speed is high. So low flight trajectories and low speed have to be applied in jump design. The inclusion of exercise regimes in ACL injury prevention to improve body position during landing was proposed by Shimokochi et al. (2013), who studied the influence of changing the sagittal plane body position (self-selected, leaning forward and upright) during single-leg landings. Based on the present results, special focus on trunk control regarding jump landing in downhill skiing is suggested.

The musculo-skeletal model had certain limitations. The model was two-dimensional and effects due to internal/external rotation and varus/valgus of the knee joint were not included, which are known to affect ligament forces (Shimokochi & Shultz, 2008). Such out-of-plane loads are likely to occur during jump landings (Bere et al., 2011a), and our findings do not directly apply to such cases. Extending the present planar model to three dimensions to investigate these out-of-plane loads additionally is in progress.

In each perturbed landing simulation, muscle stimulation patterns were re-optimized such that the skier tries an active recovery motion to regain balance. Because the optimized muscle stimulation patterns affect the corresponding muscle forces and the loading of the knee and ligaments, a sensitivity analysis was conducted to test whether the optimized muscle stimulation patterns are affected by the choice of the objective function. The analysis showed that changing the weight factor \( w_{\text{mus}} \) by a factor of 2 (setting \( w_{\text{mus}} \) to 0.5 and 2, respectively) in a sample of 100 perturbed landing simulations only changed the force in the ACL on average by 4%. Regaining a balanced position represents the behavior that would be expected from a real skier who finds him/herself in a perturbed position prior to ground contact. Up to the authors’ knowledge, this is the first study, where a series of perturbed landing simulations with a given task has been solved. The conventional approach has been to generate repeated forward simulations with the same muscle excitation patterns (McLean et al., 2004, 2008) or to use a prescribed muscle excitation
pattern (Gerritsen et al., 1996). However, both approaches neglect task-oriented adaptive behavior of the athlete.

In the series of Monte Carlo simulations, the joint angles and trunk orientation were perturbed prior to ground contact, and not the velocities. Variation of the linear velocity of the trunk segment normal to the snow surface could be used to include the influence of jump height. However, measurement data regarding variation of jump heights in downhill skiing are currently lacking. Further applications of the present musculo-skeletal model might be to study the effect of the inclination of the landing surface, the speed, and the jump height of the skier as well as modifications of the equipment. In addition, alternative control strategies of the skier might also be investigated aiming at a reduction of the peak force in the ACL during jump landing.

**Perspectives**

Competitive skiers face a high injury risk during off-balance jump landing maneuvers in downhill skiing (Flørenes et al., 2009, 2012). *In vivo* studies, which mimic injury situations, are ethically not feasible. However, musculo-skeletal modeling offers the possibility to study injury situations in a computer environment. A two-dimensional musculo-skeletal skier-skis model was developed and applied to investigate a cause-and-effect relationship between landing position and peak ACL force during jump landing. Backward lean of the skier was identified as the most important predictor for high ACL forces. An increase of hip flexion, knee extension, ankle dorsiflexion, and an asymmetric position were also related to higher peak ACL forces. These results are in agreement with previous simulation results (Gerritsen et al., 1996) and video sequences of injury cases during landing movements in competitive downhill skiing (Bere et al., 2011a). The inclusion of exercise regimens in ACL injury prevention programs with special focus on trunk control and a set of preventive measures were suggested. Further applications of the present model might be to study the effect of jump height and speed, modifications of the equipment, and neuromuscular control strategies aiming at the prediction of ACL risk factors during jump landing in downhill skiing.

**Key words:** skiing, simulation, musculo-skeletal modeling, multiple regression.

**Supporting Information**

Additional Supporting Information may be found in the online version of this article at the publisher’s web-site:

**Video S1.** Animation of the baseline landing simulation.

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**References**


